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Quantum erasing of laser emission in N₂⁺

Rostyslav Danylo 1,2 , Guillaume Lambert 1 , Yi Liu 2,3 , Vladimir Tikhonchuk 4,5 , Aurélien Houard 1 , and André Mysyrowicz 1,*

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Cavity-free lasing of N_2^+ induced by a femtosecond laser pulse at 800 nm is nearly totally suppressed by a delayed twin control pulse. We explain this surprising effect within the V-scheme of lasing without population inversion. A fast transfer of population between nitrogen ionic states $X^2\Sigma_g^+$ and $A^2\Pi_u$, induced by the second pulse, terminates the conditions for amplification in the system. Appearance of short lasing bursts at delays corresponding to revivals of rotational wave packets are explained along the same lines.

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1. INTRODUCTION

According to quantum mechanics, electronic transitions are described not by probabilities but by *amplitudes* of probabilities. This leads to the possibility, when two electronic levels are coupled to a common third level by coherent radiation fields, of interference effects with unusual consequences. Counterintuitive effects such as suppression of spontaneous emission [1], induced transparency of an opaque medium [2, 3] or lasing without population inversion [4, 5] have been reported. Recently, we have interpreted the cavity-free lasing of N_2^+ pumped by femtosecond laser pulses as being due to such a lasing without population inversion [6, 7]. Here we report a peculiar consequence from quantum interference in this system, namely the quenching of this laser emission when a second delayed femtosecond pump pulse is injected in the gas.

2. RESULTS AND DISCUSSION

The erasing effect is shown in Figure 1. A laser pump pulse of 45 fs duration and 1 mJ energy with central wavelength at 800 nm is focused with a 40 cm lens (NA = 0.0125) in a 1 m length gas chamber filled with nitrogen gas at low pressure

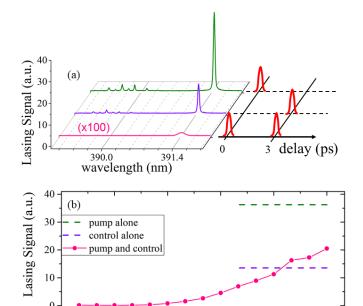


Fig. 1. a) Time-integrated lasing signal in the forward direction obtained with a 800 nm pump pulse of 45 fs duration, NA=0.0125. Each measurement is averaged over 1000 laser shots. Upper trace (green curve): pump pulse only (1 mJ energy), middle trace (violet curve): delayed control pulse only (1 mJ energy), lower trace (pink curve): consecutive pump and control 1 mJ pulses with 3 ps delay. b) Time-integrated lasing signal at 391.4 nm plotted as a function of delay dt between the pump and control pulses. The N_2 gas pressure is 30 mbar.

time (ps)

(30 mbar). It leads to the formation of a plasma channel about 1 cm in length and to cavity-free self-seeded lasing at 391.4 nm in the direction of the pump pulse (Figure 1a, upper trace). The 391.4 nm wavelength corresponds to a transition between second excited state $B(\nu=0)$ and ground state $X(\nu=0)$ of N_2^+ [8–20].

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As expected, another pulse, hereafter called control pulse, of same energy and duration gives a signal of same order (Figure 1a, middle trace). A small difference in the intensities of pump and control pulses explains the slight difference in lasing signals since self-seeded gain at 391.4 nm is very high, the lasing signal increasing by 3 orders of magnitude when the pump pulse is increased by a factor from 2 to 3. However, when both pump and control pulses are sent consecutively within a few picoseconds, one observes a reduction by a factor ~ 1000 of the global lasing output, as shown in Figure 1a, lower trace. This surprising effect is robust, as shown in Figure 1b, where the time-integrated lasing signal at 391.4 nm is plotted as a function of time between the two 800 nm pulses. As can be seen, the erasing effect lasts for more than 5 ps, much longer than the pump or control pulse duration.

Before discussing this result, it is useful to describe the properties of 800 nm femtosecond pulse-induced N₂⁺ lasing and its interpretation. Cavity-free lasing in the forward direction happens within the plasma column created in air or pure nitrogen gas by an intense femtosecond laser pulse with peak intensity $\sim 10^{14}$ W/cm². The emitted lasing pulse at 391.4 nm is retarded from the pump pulse by several picoseconds and its duration varies between 1-2 ps and 10 ps or more near lasing threshold, depending on pressure [17]. This behavior is typical for the collective emission of many emitters locked to a common phase [21]. Injection of a weak femtosecond seed pulse at 391 nm amplifies the signal by 2-3 orders of magnitude [9, 10, 15, 17]. Three models have been proposed to interpret this cavity-free lasing [6, 10, 11, 14]. Noting that the pump pulse at 800 nm is quasiresonant with intermediate ionic level A ($A^2\Pi_u$), a first model assumes that fast depletion of the ionic ground state X leads to a population inversion between levels B and X [11-13]. However, this model does not explain the retarded emission of the lasing signal nor its dependence with gas pressure. A second model assumes no electronic population inversion and attributes the lasing to an inversion of rotational states of levels B and X [14]. However, it ignores the role of pressure, of resonant intermediate level A and the effects of propagation of the lasing signal through the sample. We have recently developed another model that does not require electronic or rotational population inversion between initial state B and final state X for the initiation of lasing [6, 7]. This third interpretation relies on the observation of long-lived coherent polarizations X-A and X-B subsisting in the system well after the passage of the pump pulse [6]. Coupling between these polarizations in a V-scheme arrangement (see Figure 1 in Ref. [6]) maintained by a weak laser post-pulse, leads to the possibility of amplification of the B-X transition in the absence of population inversion ($n_B < n_X$). In this case, a softer condition for amplification requires $n_B > n_A$. Simulations based on Maxwell-Bloch equations, discussed in Ref. [6] and in more details in Ref. [7] in which rotational effects are included, restitute well the measured temporal shape of the lasing emission and the lasing response as a function of gas pressure.

The gain can be expressed as [7]:

$$E_b x = E_b x^0 \exp\left(\frac{\mu_{ax}\mu_{bx}E_p^0}{3\hbar \mid \omega_{ax} - \omega_p \mid} \sqrt{\frac{N_i(n_B - n_A)\omega_{bx}\tau z}{c\epsilon_0 \hbar}}\right)$$
 (1)

where E_{bx}^0 and E_{bx} are the fields for the B-X transition at the beginning and at the end of the plasma column, ω_{ax} and ω_{bx} are the transition frequencies, μ_{ax} =0.25 at.u. and μ_{bx} =0.75 at.u.

are the corresponding dipole moments, ω_p and E_p^0 are the frequency and amplitude of the laser post-pulse, z is the length of the plasma column, $\tau=t-z/c$ is the co-propagating time, N_i is the density of N_2^+ ions, ϵ_0 is the vacuum permittivity and \hbar is the Planck constant. The intensity and duration of the post pulse were obtained from the experiment. According to our model that includes the five resonant electronic levels B ($\nu=0$), X ($\nu=0$), X ($\nu=1$), A ($\nu=2$) and A ($\nu=3$), the repartition of ionic populations at the end of a 40 fs pump pulse with 2.5 × 10^{14} W/cm² peak intensity is the following: $n_X(\nu=0)=31\%$, $n_X(\nu=1)=21\%$, $n_B=19\%$, $n_A(\nu=2)=16\%$ and $n_A(\nu=3)=13\%$. At the end of the lasing signal at 391.4 nm, the population at level B has decreased by 2% and the population at level A has increased by 30% so that the lasing emission has been interrupted because condition $n_A< n_B$ was no more fulfilled.

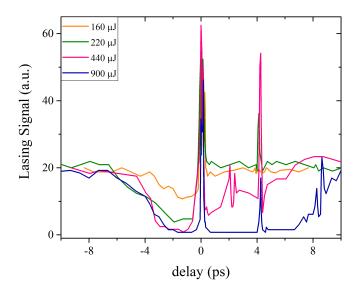


Fig. 2. Time-integrated lasing signal obtained with consecutive pump and control pulses. Pump pulse has 1.1 mJ energy, control pulse energy is indicated in the legend, NA=0.01. N_2 gas pressure is 100 mbar.

A clue to the origin of the quenching effect due to the control pulse is given in Figure 2. The lasing signal is shown as a function of delay between 800 nm pump and control pulses, for different energies, and consequently intensities, of the weaker control pulse, starting with an intensity below that required for high field ionization of the nitrogen gas. Positive delay dt in Figure 2 corresponds to the weaker control pulse arriving first in the gas chamber. Inspecting first the lowest control pulse intensity, a reduction of lasing signal (due solely to the more intense pump pulse) appears only for dt < 0, when the weaker control pulse follows the stronger pump pulse, while the amount of lasing for dt > 0 is not affected. It indicates that the lasing partial quenching corresponds to an interaction of the control pulse with the plasma generated by the first IR pulse. Noting that the pump pulse wavelength at 800 nm is quasi-resonant with the $X(\nu = 0) \rightarrow A(\nu = 2)$ transition, we interpret the lasing erasing effect as due to a fast transfer of population from X to A, interrupting the coherent emission when the condition $n_A = n_B$ is reached. This leads to a quenching of the lasing signal, which obviously cannot last longer than duration of lasing. According to Ref. [17] and to the theoretical model of Ref. [7] the duration of the B-X lasing is about 10 ps for a gas pressure

of 30 mbar, and it decreases to 4 ps when the pressure increases to 100 mbar. Figure 2 also shows how the lasing signal depends on the intensity of the control 800 nm pulse. For dt < 0, the duration of quenching does not change appreciably, because it is essentially determined by the lasing duration of the stronger pulse, as discussed above. By contrast, for dt > 0 we observe a longer duration at the highest control pulse intensities. This can be understood by the fact that the transfer of population $X \rightarrow A$ responsible for quenching can now occur during the plasma lifetime created by the control pulse, which is longer than the lasing duration. We have verified that the quenching duration increases also for dt < 0 when the collected lasing signal has a significant contribution from both pulses.

In addition to the quenching effect, Figure 2 demonstrates the appearance of sharp emission maxima and minima for dt > 00. This effect is shown in more details in Figure 3 for pump and control pulses having parallel and orthogonal polarizations. Note that the lasing spikes seen in Figure 2 and 3 do not appear in Figure 1b because of the poorer scan resolution (1ps). To explain the appearance of lasing signals during these short time intervals (few hundreds of femtoseconds), two additional, well documented effects must be taken into account: the preparation of coherent rotational wave packets by the first pulse and the $X \rightarrow A$ selection rule that forbids (allows) the $X \rightarrow A$ transition when the field is parallel (perpendicular) to the molecular ion axis. A coherent rotational wave packet is induced in neutral nitrogen molecules by an intense short laser pulse that aligns them partially along the laser field. Because of inertia, a first alignment occurs ~100 fs after the laser peak. Spontaneous revivals of rotational wave packets and concomitant realignment of neutral molecules occur with a specific period T = 1/4Bc =4.166 ps, where $B = 2 \text{ cm}^{-1}$ is the rotational constant of N_2 and cthe speed of light, first along the laser field of the first pulse and then alternatively parallel and perpendicular to it [14, 22, 23].

Let us examine the case of a second pulse with a polarization parallel to the first pulse impinging with a delay corresponding to a revival. Because of the anisotropic polarizability of N_2 , during the short time ~ 100 fs of the revival, the second pulse preferentially ionizes neutral molecules that are aligned along the first laser field. Therefore all ions, which are formed around the peak of the pulse predominantly in state X, become themselves aligned along the first pulse field. The quenching effect is inoperative for this alignment of the ions since the $X \rightarrow A$ transition is forbidden when the electric field is parallel to the molecule axis. This synchronization explains the appearance of a lasing signal for this particular time delay. This is an efficient, phase-matched process, in the sense that the second pulse always encounters this favorable alignment of ionized molecules during its propagation through the sample. The recurrence time of lasing revivals shown in Figure 3 is in excellent agreement with the time of partial alignment of the neutral molecules along the laser field calculated in reference [14]. It is worth stressing that ions are responsible for the appearance of the lasing peaks even though the recurrence period corresponds to rotation of neutral molecules. When the ions are aligned perpendicular to the first pulse field, a sign reversal is observed, lasing minima replacing lasing maxima. The same explanation holds. For molecules aligned perpendicular to the field of the first pulse, the $X\rightarrow A$ transition is now allowed (the second pulse field is perpendicular to the molecules axis). The quenching effect is therefore reinforced. The positions of quenching minima are again in excellent agreement with the calculated alignments of molecules perpendicular to the first field. Finally, we have veri-

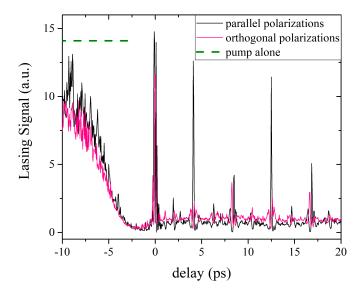


Fig. 3. Time-integrated lasing signal as a function of delay between consecutive pump and control pulses with parallel (in black) and orthogonal (in pink) polarizations. Pulse energies are 1.2 mJ and 0.55 mJ, the other experimental conditions are the same as in Figure 1. The dashed horizontal green line represents the magnitude of the lasing signal with 1.2 mJ pump pulse only. Maxima (minima) in pink and black curves correspond to an alignment of X ions parallel (perpendicular) to the first laser pulse field (see main text).

fied experimentally that minima replace maxima and vice-versa when pump and control pulses have orthogonal polarizations, a result explained by the same reasoning (see Figure 3).

So far we have only discussed the erasing effect of self-seeded lasing in N₂⁺. As mentioned before, an external femtosecond seed pulse around 391 nm amplifies the lasing signal by several orders of amplitude. It is interesting to verify if the quenching is still effective in this case. To answer this question experimentally, an external seed around 391 nm with \sim 200 fs duration was generated in a mismatched BBO-crystal and injected $\sim 300 \text{ fs}$ after the 800 nm pump pulse, leading to amplification of the lasing signal by a factor \sim 100. By comparison, the lasing signal from the control pulse remained negligibly small. As shown in Figure 4, a significant erasing of lasing occurred even in this case for both dt > 0 and dt < 0. In particular, lasing totally vanished for dt = -1 ps. The poorer scan resolution (500 fs instead of 50 fs scan steps in Figure 3) prevents the clear observation of lasing revivals. To sum up, our arguments about the origin of the lasing suppression remain valid in the presence of an external seed.

3. CONCLUSION

In conclusion, we have reported the nearly total quenching of cavity-free lasing of N_2^+ by two consecutive femtosecond laser pulses at 800 nm wavelength. This effect has its root in the interference between amplitudes of transitions between levels $X^2\Sigma_g^+$, $A^2\Pi_u$ and $B^2\Sigma_u^+$ of N_2^+ in a V-arrangement. The V-scheme of lasing without population inversion explains naturally the origin of this double pulse erasing process. Quenching is due to a transition from ground X to first excited state A of singly ionized nitrogen molecules induced by the control pulse, leading to an abrupt stop of the lasing when the populations of levels

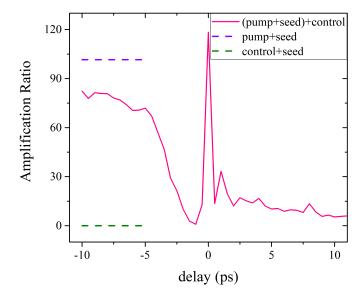


Fig. 4. Pink curve: Time-integrated amplification ratio as a function of delay between a fixed pump and a scanned control pulse at 800 nm. Pump pulse energy is 0.8 mJ. Control pulse energy is 0.7 mJ. Pulse duration is 45 fs. An external seed pulse around 391 nm with 200 fs duration is injected 300 fs after the pump pulse. Amplification ratio refers to the ratio between amplified lasing signal and injected external seed, self-seeded lasing intensity being negligible. Gas pressure is 30 mbar. Violet dash horizontal line represents the magnitude of the laser amplification for the 0.8 mJ pump pulse when the weak seed at 391 nm is injected. Green dash horizontal line gives the amplification from the control pulse (see main text for more details).

A and B become equal. The same process also explains the subtle behavior of lasing for delays between the two pump pulses corresponding to coherent wave packet revivals. We finally note that the presented results seem in contradiction with other proposed models [11-14]. In the model based on population inversion between B and X, which has the merit to have pointed out first the role of intermediate level A, a second pulse at 800 nm with a short delay should further deplete level X in a X-A transition and consequently should lead to an increase, not a decrease of lasing signal. The rotation inversion model predicts gain windows that are slightly shifted in time from the lasing revival times observed here. It does not explain the quenching effect. In our opinion rotation level inversion is not at the origin of lasing in N2 although the model is certainly valuable in explaining a reinforcement of the lasing at certain delays.

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